

Package ‘OEFPIL’

October 12, 2022

Type Package

Title Optimal Estimation of Function Parameters by Iterated Linearization

Version 0.1.1

Description Package for estimating the parameters of a nonlinear function using iterated linearization via Taylor series. Method is based on Kubáček (2000) ISBN: 80-244-0093-6. The algorithm is a generalization of the procedure given in Köning, R., Wimmer, G. and Witkovský, V. (2014) <[doi:10.1088/0957-0233/25/11/115001](https://doi.org/10.1088/0957-0233/25/11/115001)>.

License GPL (>= 2)

Depends R(>= 3.6.0)

Imports Deriv, MASS, ggplot2, matrixcalc, minpack.lm, plyr

Encoding UTF-8

LazyData true

RoxygenNote 7.1.2

NeedsCompilation no

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Repository CRAN

Date/Publication 2021-11-04 15:00:02 UTC

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coef.OEFPIL	<i>Extract model coefficients from OEFPIL</i>
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Description

Function which extracts the estimated model coefficients from an object of class "OEFPIL".

Usage

```
## S3 method for class 'OEFPIL'
coef(object, ...)
```

Arguments

object	an object of class "OEFPIL" (a result of a call to OEFPIL).
...	other arguments.

Value

A named vector of estimated model coefficients extracted from an "OEFPIL" object.

See Also

[OEFPIL](#)

Examples

```
##Creating a data file (using steam data from MASS library)
library(MASS)
steamdata <- steam
colnames(steamdata) <- c("x", "y")
startsteam <- list(b1 = 5, b2 = 8, b3 = 200)
k <- nrow(steamdata)
CM <- diag(rep(0.1, 2*k))
```

```
##Creating an OEFPIL object
st1 <- OEFPIL(steamdata, y ~ b1 * 10^(b2 * x/ (b3 + x)), startsteam, CM, useNLS = FALSE)

##Use of coef function
coef(st1)
```

confBands.OEFPIL *Confidence and prediction bands for OEFPIL object*

Description

Function calculates pointwise confidence bands and prediction bands of estimated function from an object of class "OEFPIL".

Usage

```
## S3 method for class 'OEFPIL'
confBands(object, xx, signif.level = 0.05, new.obs.variance)
```

Arguments

object	an object of class "OEFPIL" (a result of a call to OEFPIL).
xx	a sequence of x-coordinates of points for computing confidence and prediction intervals. If missing, the default sequence <code>seq(from = min(x), to = max(x), length.out = 301)</code> is used.
signif.level	a numerical value or a vector of significance levels for confidence bands. If missing, the default value 0.05 is used.
new.obs.variance	the variance of a new observation for prediction interval computing.

Details

An argument `signif.level` can be one numerical value or vector of numerical values of significance levels for confidence intervals.

If `new.obs.variance` is not defined by user, the average variance in the dependent variable is used to compute prediction intervals.

Value

Returns an object of type list containing the following components.

xx	a numerical vector of points where intervals are calculated.
yy	a numerical vector with values of estimated function in xx.
PointwiseCB	a matrix of confidence intervals at points xx.
PredictCB	a matrix of prediction intervals at points xx.

See Also

[OEFPIIL](#), [plot.OEFPIIL](#)

Examples

```
##-- Continuing the coef.OEFPIIL(.) example:

##Use of confBands function with default parameters
a <- confBands(st1)
str(a)

##Computing two different confidence bands in one step
b <- confBands(st1, signif.level = c(0.01,0.05))
str(b)
```

confInt.OEFPIIL	<i>Confidence intervals for OEFPIIL parameters</i>
-----------------	--

Description

Function computes confidence intervals for the parameters counted by OEFPIIL function.

Usage

```
confInt.OEFPIIL(object, signif.level = object$contents$signif.level, parm)
```

Arguments

object	an object of class "OEFPIIL" (a result of a call to OEFPIIL).
signif.level	a numerical value or a vector of significance levels for confidence intervals. If missing, a value from the input "OEFPIIL" object is used.
parm	a specification of which parameters are to be given confidence intervals, either a vector of numbers or a vector of names. If missing, all parameters are considered.

Details

The confidence intervals are computing under normality assumption.

Value

A matrix of estimated confidence intervals for model coefficients from an "OEFPIIL" object. The matrix contains lower and upper confidence limits (columns) for each parameter (rows).

See Also[OEFPIL](#)**Examples**

```
##-- Continuing the coef.OEFPIL(.) example:

##Use of confint function
#one numerical value
confInt.OEFPIL(st1)

#vector of numerical values
confInt.OEFPIL(st1, signif.level = c(0.01,0.05,0.1))

#estimation of specified parameters
confInt.OEFPIL(st1 , signif.level = c(0.01,0.05,0.1), parm = c('b1', 'b2'))
```

curvplot.OEFPIL *Plot of estimated curve for OEFPIL object*

Description

Function for plotting the estimated curve with pointwise confidence bands for an object of class "OEFPIL".

Usage

```
curvplot.OEFPIL(object, signif.level, xx)
```

Arguments

object	an object of class "OEFPIL" (a result of a call to OEFPIL).
signif.level	a numeric value or a vector of significance levels for pointwise confidence bands. If missing, the estimated curve is plotted without confidence bands.
xx	a sequence of x-coordinates of points for computing and plotting confidence bands. If missing, the default sequence seq(from = min(x), to = max(x), length.out = 301) is used.

Value

A ggplot graph of the estimated curve with pointwise confidence bands. The result can be edit using other ggplot components as usually.

See Also

[OEFPIL](#), [paramplot.OEFPIL](#) and [plot.OEFPIL](#).

Examples

```

library(MASS)
library(ggplot2)

##Creating a data file
steamdata <- steam
colnames(steamdata) <- c("x","y")
n <- nrow(steamdata)
CM1 <- diag(rep(10,2*n))
CM2 <- diag(c(rep(12,n), rep(14,n)))

##Creating OEFPIIL objects
st1 <- OEFPIIL(steamdata, y ~ b1 * 10^(b2 * x/ (b3 + x)), list(b1 = 5, b2 = 8, b3 = 200),
              CM1, useNLS = FALSE)
st2 <- OEFPIIL(steamdata, y ~ b1 * 10^(b2 * x/ (b3 + x)), list(b1 = 5, b2 = 8, b3 = 200),
              CM2, useNLS = FALSE)

##Use of curvplot.OEFPIIL function on an object of class 'OEFPIIL'
curvplot.OEFPIIL(st1, signif.level = 0.05)

##Use of curvplot.OEFPIIL function on an object of class 'OEFPIIL' with different arguments
curvplot.OEFPIIL(st2, signif.level = c(0.01,0.05), xx = seq(0,110,1))

##Use of curvplot.OEFPIIL function with additional arguments as for ggplot2
curvplot.OEFPIIL(st1, signif.level = 0.05) +
  labs(x = "New x label") +
  labs(title = "New graph title")

```

 NanoIndent.OEFPIIL

Estimation of parameters in nanoindentation

Description

Fitting the unloading curve in nanoindentation process by power law function with parameters estimated by iterated linearization algorithm (OEFPIIL). The special case of [OEFPIIL](#) function customized for using in nanoindentation (see 'Details').

Usage

```

NanoIndent.OEFPIIL(data, alpha.start, m.start, hp.start, unload.data = FALSE, ucut = 0.98,
                  lcut = 0.4, CM, uh = 0.5, uF = 0.001, max.iter = 100,
                  see.iter.val = FALSE, save.file.name, th = .Machine$double.eps ^ (2 / 3),
                  signif.level = 0.05, useNLS = TRUE)

```

Arguments

data	an object of type data.frame with 2 named columns or list with 2 elements.
alpha.start	a starting value of the fitting constant alpha.

<code>m.start</code>	a starting value of the exponent <code>m</code> .
<code>hp.start</code>	a starting value of the permanent indentation depth <code>hp</code> .
<code>unload.data</code>	a logical value (default FALSE) indicating the structure of data. If TRUE, an input data contains only unloading part of the curve. If FALSE, an input data contains complete loading, hold and unloading parts of an indentation process.
<code>ucut</code>	a numerical value, indicating the upper bound of cut off.
<code>lcut</code>	a numerical value, indicating the lower bound of cut off.
<code>CM</code>	a covariance matrix of the input data. See 'Details' for more information.
<code>uh</code>	standard deviation of depth.
<code>uF</code>	standard deviation of load.
<code>max.iter</code>	maximum number of iterations.
<code>see.iter.val</code>	logical. If TRUE, all the partial results of the OEFPIIL algorithm are displayed and saved. The default value is FALSE.
<code>save.file.name</code>	a name of the file for saving results. If missing, no output file is saved.
<code>th</code>	a numerical value, indicating threshold necessary for the iteration stoppage.
<code>signif.level</code>	a significance level for the confidence interval.
<code>useNLS</code>	logical. If TRUE (the default value), function will set up starting parameters calculated by <code>nlsLM</code> function (nonlinear least square estimation).

Details

In this special case of the OEFPIIL function, the dependence of parameters is fixed in the form: $F = \alpha * (h - h_p)^m$, where F is load and h depth measured within a nanoindentation process. It is possible to set own starting values of the parameters, in the other case these values are calculated by the algorithm and printing into the console.

A selection of the part of the unloading curve fitted by a power law function is provided with `lcut` and `ucut` arguments. The default values 0.4 and 0.98 corresponds to the range 40-98 % F_{max} (maximum force) as recommended in ISO 14577 standard.

The `CM` has to be a $2n$ covariance matrix (where n is length of data) of following structure: first n elements of the diagonal correspond to the variance of depth and other to the variance of load. If argument `CM` is missing, the input covariance matrix is set to a diagonal matrix with variance of depth and load (calculated from `uh` and `uF`) on the diagonal. If standard deviations are missing too, the default values (`uh=0.5`, `uF=0.001`) are used.

The estimations and confidence intervals are computed under normality assumption (see OEFPIIL 'Details').

Value

Returns an object of class "OEFPIIL". It is a list containing at least the following components

<code>name_Est</code>	estimations of model parameters.
<code>name_upgraded.start.val</code>	modified starting values of estimating parameters (result from <code>nlsLM</code> function).
<code>cov.m_Est</code>	estimated covariance matrix of parameters.

it_num	number of iterations.
CI_parameters	a list of confidence intervals for estimated parameters (a significance level is based on signif.level argument).
logs	warnings or messages of events, which happen during the run of the algorithm.
...	for other components specification see OEFPIIL .
contents	a list of outputs as original values of data and other characteristics, which are usable in plotting or other operations with model results.

If useNLS argument is set to FALSE, the name_upgraded.start.val are the same as start.values (no nlsLM procedure for starting value fitting is performed).

References

ISO/IEC: 14577-1:2015 *Metallic materials – Instrumented indentation test for hardness and materials parameters – Part 1: Test method* (ISO/IEC, International Organisation for Standardisation, 2015).

Anna Charvátová Campbell, Petr Grolich, Radek šlesinger. (2019). *Niget: Nanoindentation general evaluation tool*. SoftwareX, **Vol. 9**: 248–254. doi: [10.1016/j.softx.2019.03.001](https://doi.org/10.1016/j.softx.2019.03.001).

Köning, R., Wimmer, G. and Witkovský, V. *Ellipse fitting by nonlinear constraints to demodulate quadrature homodyne interferometer signals and to determine the statistical uncertainty of the interferometric phase*. Measurement Science and Technology (2014).

See Also

[OEFPIIL](#)

Examples

```
##Use of NanoIndent function for data file "silicaBerk.RData" (a part of the OEFPIIL package)
signif.level = 0.05
output.form.NI <- NanoIndent.OEFPIIL(silicaBerk, unload.data = TRUE, ucut = 0.98, lcut = 0.2,
uh = 0.5, uF = 0.001, signif.level = signif.level)

##The output is an object of class 'OEFPIIL', supplementary functions for this class are available
##Use of summary function
summary(output.form.NI)

##Plot of estimated unloading curve
plot(output.form.NI, signif.level = signif.level)
```


Description

Function for computing optimal estimate of parameters of a nonlinear function by iterated linearization (using Taylor expansion). The model considers measurements errors in both (dependent and independent) variables.

Usage

```
OEFPIIL(data, form, start.val, CM, max.iter = 100, see.iter.val = FALSE,
        save.file.name, th, signif.level, useNLS = TRUE)
```

Arguments

<code>data</code>	a data file can be any object of type <code>data.frame</code> with 2 named columns or <code>list</code> with 2 elements.
<code>form</code>	an object of class <code>formula</code> (or one that can be coerced to that class): a symbolic description of the model to be fitted. The details of model specification are given under 'Details'.
<code>start.val</code>	a named list of starting values of estimating parameters.
<code>CM</code>	a covariance matrix of data (See 'Details' for the information about required structure.).
<code>max.iter</code>	maximum number of iterations.
<code>see.iter.val</code>	logical. If TRUE, all the partial results of the algorithm are displayed and saved. The default value is FALSE.
<code>save.file.name</code>	a name of the file for saving results. If missing, no output file is saved.
<code>th</code>	a numerical value, indicating threshold necessary for the iteration stoppage. The default value is $.Machine$double.eps^{(2/3)}$.
<code>signif.level</code>	a significance level for the confidence interval. If missing, the default value 0.05 is used.
<code>useNLS</code>	logical. If TRUE (the default value), function will set up starting parameters calculated by <code>nlsLM</code> function (nonlinear least square estimation).

Details

Models for OEFPIIL function are specified symbolically. A typical model has the form $y \sim f(x, a_1, \dots, a_n)$, where

- y is the (numerical) response vector,
- x is the predictor,
- terms a_1, \dots, a_n are parameters of specified model.

Function f is known nonlinear function with continuous second partial derivatives with respect to x and parameters a_1, \dots, a_n (for more details see (Kubáček, 2000)).

All calculations are performed assuming normality of a response vector and measurements errors.

In the data entry of type `data.frame`, both columns must be named as variables in formula. The same holds for elements of `list`.

A choice of `start.val` is important for the convergence of the algorithm. If the OEFPIIL algorithm does not converge, starting values modified by `nlsLM` function (`useNLS = TRUE`) are recommended (see Example 3).

The CM has to be a $2n$ covariance matrix (where n is length of data) of following structure: first n elements of the diagonal correspond to the variance of independent variable (x) and other to the variance of dependent variable (y). If argument CM is missing, the input covariance matrix is set to a diagonal variance matrix with sample variance on the main diagonal.

Value

Returns an object of class "OEFPIIL". It is a list containing the following components

<code>name_Est</code>	estimations of model parameters.
<code>name_upgraded.start.val</code>	modified starting values of estimating parameters (result from <code>nlsLM</code> function).
<code>cov.m_Est</code>	estimated covariance matrix of parameters.
<code>cov.m_nlsLM</code>	a covariance matrix of starting values of parameters from <code>nlsLM</code> function (if <code>useNLS</code> was set to <code>TRUE</code>).
<code>it_num</code>	number of iterations.
<code>name_previous.step</code>	the parameter values from the previous iterative step.
<code>CI_parameters</code>	a list of confidence intervals for estimated parameters (a significance level is based on <code>signif.level</code> argument).
<code>logs</code>	warnings or messages of events, which happen during the run of the algorithm.
<code>contents</code>	a list of outputs as original values of data and other characteristics, which are usable in plotting or other operations with model results.

If `useNLS` argument is set to `FALSE`, the `name_upgraded.start.val` are the same as `start.values` (no `nlsLM` procedure for starting value fitting is performed).

Note

The symbol π is reserved for the Ludolf's constant. So naming one of the model's parameters by this symbol results in constant entry of the model.

References

- Kubáček, L. and Kubáčková, L. (2000) *Statistika a metrologie*. Univerzita Palackého v Olomouci.
- Köning, R., Wimmer, G. and Witkovský, V. (2014) *Ellipse fitting by nonlinear constraints to demodulate quadrature homodyne interferometer signals and to determine the statistical uncertainty of the interferometric phase*. Measurement Science and Technology.

See Also

[NanoIndent.OEFPIIL](#) and function `nlsLM` from `minpack.lm` package for nonlinear least square algorithms.

Examples

```
##Example 1 - Use of OEFPIIL function for steam data from MASS library
library(MASS)
steamdata <- steam
colnames(steamdata) <- c("x","y")
k <- nrow(steamdata)
CM <- diag(rep(5,2*k))

st1 <- OEFPIIL(steamdata, y ~ b1 * 10 ^ (b2 * x/ (b3 + x)),
  list(b1 = 5, b2 = 8, b3 = 200), CM, useNLS = FALSE)

## Displaying results using summary function
summary(st1)

## Plot of estimated function
plot(st1, signif.level = 0.05)

## Example 2 - Use of OEFPIIL for nanoindentation data "silica2098.RData"
## (which is part of the OEFPIIL package)
## Preparing arguments for OEFPIIL function
max.iter = 100
see.iter.val = FALSE
signif.level = 0.05
useNLS = TRUE

## Creating a list with starting values for parameters
start.val <- list(alpha=0.1, m=1.5, hp=0.9)
names(start.val) <- c("alpha", "m", "hp")

## Imputed formula
form <- Load ~ alpha * (Depth - hp) ^ m
k <- length(silica2098[,1])
CM <- diag(c(rep(0.5^2,k),rep(0.001^2,k)))

## Use of OEFPIIL function with defined arguments
output.form <- OEFPIIL(silica2098, form, start.val, CM = CM, max.iter = max.iter,
  see.iter.val = see.iter.val, signif.level = signif.level, useNLS = useNLS)

## Displaying results with summary (the result is the same as in NanoIndent.OEFPIIL function)
summary(output.form)
```

Description

Function for calculating orthogonal residuals of an "OEFPIL" object (i.e. the shortest Euclidean distance between data points and the estimated function from OEFPIL).

Usage

```
ortresiduals.OEFPIL(object, min.c)
```

Arguments

object	an object of class "OEFPIL" (a result of a call to OEFPIL).
min.c	a numeric value, for defining minimization interval for the optimize function (if not defined, default value $0.05 * \text{range}(x)$ is used). Must be positive.

Value

Returns an object of type list containing following components

x.ores	a numerical vector of x coordinates of points, where the minimal distance is realized.
o.resid	a numerical vector of orthogonal residuals (minimal Euclidean distances between data points and estimated function).
SSort	the orthogonal sum of squares.

Note

The value min.c should not be too small. In that case the minimization interval is too narrow and the result can be misleading (see Example 3).

See Also

[OEFPIL](#)

Examples

```
##-- Continuing the coef.OEFPIL(.) example:

##Example 1 Use ortresiduals.OEFPIL function on the OEFPIL object, with specified value 'min.c'
ortresiduals.OEFPIL(st1,5)

##Example 2 Use ortresiduals.OEFPIL function without value 'min.c' (default.value = 0.05 * range(x))
ortresiduals.OEFPIL(st1)

##Example 3 Choice of too narrow interval. Misleading result!
ortresiduals.OEFPIL(st1,0.5)
```

paramplot.OEFPIL *Plot parameters of an OEFPIL object*

Description

Function for plotting the estimated values of the parameters with error bars (plus minus standard deviation) using ggplot for an object (or list of objects) of class "OEFPIL".

Usage

```
paramplot.OEFPIL(object)
```

Arguments

object an object or a list of objects of class "OEFPIL" (a result of a call to [OEFPIL](#)).

Details

The input list has to be without NaN, NA, Inf or -Inf values in the estimated parameters or covariance matrix in the source "OEFPIL" object. In that case the function returns a warning message and no graph is plotted.

Value

A ggplot graph of the estimated parameter values with error bars. The result can be edit using other ggplot components as usually.

Note

Due to possible large differences in units of estimated parameters, the scale argument for facetting in the ggplot graph is set to "free". It should be taken into account when interpreting the results.

See Also

[OEFPIL](#), [curvplot.OEFPIL](#) and [plot.OEFPIL](#).

Examples

```
##-- Continuing the coef.OEFPIL(.) example:

n <- nrow(steamdata)
CM2 <- diag(c(rep(0.2^2,n), rep(0.1^2,n)))
st2 <- OEFPIL(steamdata, y ~ b1 * 10^(b2 * x / (b3 + x)), list(b1 = 5, b2 = 8, b3 = 200),
             CM2, useNLS = FALSE)

##Example 1 - Use of paramplot.OEFPIL function on an object of class 'OEFPIL'
paramplot.OEFPIL(st2)
```

```
##Example 2 - Use of paramplot.OEFPIL function on a list of objects of class 'OEFPIL'
paramplot.OEFPIL(list(st1,st2))
```

```
plot.OEFPIL
```

Plot the estimate from an OEPFIL object

Description

Plot of the iterated linearization estimate of a function from an "OEFPIL" object with pointwise confidence and prediction bands.

Usage

```
## S3 method for class 'OEFPIL'
plot(x, xx, signif.level, interval, new.obs.variance, ...)
```

Arguments

x	an object of class "OEFPIL" (a result of a call to OEFPIL).
xx	a sequence of x-coordinates of points for computing and plotting confidence bands. If missing, the default sequence <code>seq(from = min(x), to = max(x), length.out = 301)</code> is used.
signif.level	a numerical value or a vector of significance levels for confidence bands.
interval	a character vector. It states type of an interval to draw. Following values are possible: "conf" for confidence interval, "pred" for prediction interval or <code>c("conf", "pred")</code> for both. If missing, no intervals are plotted.
new.obs.variance	the variance of a new observation for prediction interval computing (see confBands.OEFPIL).
...	additional arguments (same as in plot function) affecting the plot.

Details

If the `signif.level` argument is missing, even though an `interval` argument is set to "conf", the default value 0.05 is used. The line type is set to 'dashed' for confidence bands and 'dotted' for prediction bands. The confidence and prediction bands are computed under normality assumption. If the vector `signif.level` length is greater than 1, then multiple bands are plotted. The widest band has colour no. 2. The second widest band has colour no. 3 etc.

Value

Returns an object of type list containing at least the following components

xx	a numerical vector of points where bands are calculated.
yy	a numerical vector with values of estimated function in xx.
PointwiseCB	a matrix of confidence intervals at points xx.
PredictCB	a matrix of prediction intervals at points xx.

See Also[OEFPIL](#)**Examples**

```

library(MASS)

##Use of plot function with default parameters
##(only estimation of the function is plotted, without confidence or prediction bands)
steamdata <- steam
colnames(steamdata) <- c("x","y")
n <- nrow(steamdata)
CM1 <- diag(rep(10,2*n))
st1 <- OEFPIL(steamdata, y ~ b1 * 10^(b2 * x/ (b3 + x)), list(b1 = 5, b2 = 8, b3 = 200),
             CM1, useNLS = FALSE)
plot(st1)

##Use of plot function for plotting confidence bands
plot(st1, seq(0,113,0.1), signif.level = c(0.01,0.05), interval = "conf",
     main = "Graph of estimated function")

##Use of plot function for plotting prediction bands
plot(st1, seq(0,113,0.1), interval = "pred", new.obs.variance = 15)

##Return values of plot function
(a <- plot(st1, signif.level = 0.05, interval = "conf"))

```

print.OEFPIL

Print function for an object of class 'OEFPIL'

Description

Function prints the information about an object of class "OEFPIL".

Usage

```

## S3 method for class 'OEFPIL'
print(x, ...)

```

Arguments

`x` an object of class "OEFPIL" (a result of a call to [OEFPIL](#)).

`...` other arguments.

Value

Function prints short summary of "OEFPIL" object into the console. In case of assigning value into the variable, it returns object of class "OEFPIL", which is a list with components defined in [OEFPIL](#).

See Also[OEFPIIL](#)**Examples**

```
##-- Continuing the coef.OEFPIIL(.) example:  
  
##Use of print function  
print(st1)
```

`silica2098`*Nanoindentation measurements data*

Description

Load and depth measured with Berkovich diamond tip on fused silica material. Data contains only cutted part of unloading indentation curve from silicaBerk data (20-98 %, as recommended in ISO 14577 standard). The relationship between *Load* (F) and *Depth* (h) is given by equation $F = \alpha(h - h_p)^m$, where h_p is permanent indentation depth after removal of the load, α is fitting constant related to the indenter geometry and power law exponent m should be from (1,2) interval.

Usage`silica2098`**Format**

The data frame contains two columns:

Depth nanoindentation depth, in nanometers.

Load load, in milinewtons.

Source

Czech Metrology Institute, Brno, Czech Republic.

References

ISO/IEC: 14577-1:2015 *Metallic materials – Instrumented indentation test for hardness and materials parameters – Part 1: Test method* (ISO/IEC, Internation Organisation for Standardisation, 2015).

Examples

```
attach(silica2098)  
plot(Depth, Load, main = 'Graph of nanoindentation data', xlab = 'Depth (nm)', ylab = 'Load (mN)',  
col = 'darkgreen', cex = 1)
```

silicaBerk

Nanoindentation measurements data

Description

Load and depth measured with Berkovich diamond tip on fused silica material. Data contains only unloading part of indentation curve. The relationship between *Load* (F) and *Depth* (h) is given by equation $F = \alpha(h - h_p)^m$, where h_p is permanent indentation depth after removal of the load, α is fitting constant related to the indenter geometry and power law exponent m should be from (1,2) interval.

Usage

```
silicaBerk
```

Format

The data frame contains two columns:

Depth nanoindentation depth, in nanometers.

Load load, in milinewtons.

Source

Czech Metrology Institute, Brno, Czech Republic.

Examples

```
attach(silicaBerk)
plot(Depth, Load, main = 'Graph of nanoindentation data', xlab = 'Depth (nm)', ylab = 'Load (mN)',
     col = 'darkgreen', cex = 1)
```

summary.OEFPIIL

Summary from an OEFPIIL object

Description

Function for fast and clean output of all basic information of an "OEFPIIL" object.

Usage

```
## S3 method for class 'OEFPIIL'
summary(object, signif.level = object$contents$signif.level, print = TRUE, ...)
```

Arguments

object	an object of class "OEFPIL" (a result of a call to OEFPIL).
signif.level	a significance level for the confidence interval. If missing, a value from the input OEFPIL object is used.
print	print out result summaries in the console (default TRUE).
...	other arguments.

Value

Returns an object of type list containing following components

param_Est	the (numerical) vector of estimated model parameters.
sd	standard deviations for estimated model parameters.
cov.m_Est	the covariance matrix of estimated model parameters.
it_num	number of iterations.
CI_parameters	the matrix of lower and upper bounds for confidence intervals.

See Also

[OEFPIL](#)

Examples

```
##-- Continuing the coef.OEFPIL(.) example:

##Use of summary function with default parameters
summary(st1)

##Use of summary function with different parameters
summary(st1, signif.level = 0.01, print = FALSE)
```

vcov.OEFPIL

Covariance matrix from an OEFPIL object

Description

Function for extracting the estimated covariance matrix from an object of class "OEFPIL".

Usage

```
## S3 method for class 'OEFPIL'
vcov(object, ...)
```

Arguments

object an object of class "OEFPIIL" (a result of a call to [OEFPIIL](#)).
... other arguments.

Value

A matrix of the estimated covariances between the parameter estimates from an "OEFPIIL" object.

See Also

[OEFPIIL](#)

Examples

```
##-- Continuing the coef.OEFPIIL(.) example:  
  
##Use of vcov function  
vcov(st1)
```

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