

# Package ‘kcpRS’

October 25, 2023

**Type** Package

**Title** Kernel Change Point Detection on the Running Statistics

**Version** 1.1.1

**Maintainer** Kristof Meers <kristof.meers+cran@kuleuven.be>

**Description** The running statistics of interest is first extracted using a time window which is slid across the time series, and in each window, the running statistics value is computed. KCP (Kernel Change Point) detection proposed by Arlot et al. (2012) <[arXiv:1202.3878](https://arxiv.org/abs/1202.3878)> is then implemented to flag the change points on the running statistics (Cabrieto et al., 2018, <[doi:10.1016/j.ins.2018.03.010](https://doi.org/10.1016/j.ins.2018.03.010)>). Change points are located by minimizing a variance criterion based on the pairwise similarities between running statistics which are computed via the Gaussian kernel. KCP can locate change points for a given k number of change points. To determine the optimal k, the KCP permutation test is first carried out by comparing the variance of the running statistics extracted from the original data to that of permuted data. If this test is significant, then there is sufficient evidence for at least one change point in the data. Model selection is then used to determine the optimal  $k > 0$ .

**License** GPL (>= 2)

**Encoding** UTF-8

**LazyData** true

**Imports** Rcpp (>= 1.0.0)

**Depends** RColorBrewer, stats, utils, graphics, roll, foreach,  
doParallel

**Suggests** testthat (>= 3.0.0)

**Config/testthat/edition** 3

**LinkingTo** Rcpp

**RoxygenNote** 7.2.3

**NeedsCompilation** yes

**Author** Jedelyn Cabrieto [aut],  
Kristof Meers [aut, cre],  
Evelien Schat [ctb],  
Janne Adolf [ctb],

Peter Kuppens [ctb],  
Francis Tuerlinckx [ctb],  
Eva Ceulemans [ctb]

**Repository** CRAN

**Date/Publication** 2023-10-25 13:10:02 UTC

## R topics documented:

kcpRS-package . . . . .	2
CO2Inhalation . . . . .	3
getScatterMatrix . . . . .	4
kcpa . . . . .	5
kcpRS . . . . .	5
kcpRS_workflow . . . . .	8
MentalLoad . . . . .	10
permTest . . . . .	10
runAR . . . . .	12
runCorr . . . . .	12
runMean . . . . .	13
runVar . . . . .	14

**Index** **15**

---

kcpRS-package	<i>KCP on the running statistics</i>
---------------	--------------------------------------

---

## Description

Flagging change points on a user-specified running statistics through KCP (Kernel Change Point) detection. A KCP permutation test is first implemented to confirm whether there is at least one change point ( $k>0$ ) in the running statistics. If this permutation test is significant, a model selection procedure is implemented to choose the most optimal number of change points.

## Details

This package contains the function [kcpRS](#) that can accept a user-defined function, `RS_fun`, which should derive the running statistics of interest. For examples, see [runMean](#), [runVar](#), [runAR](#) and [runCorr](#). `kcpRS` performs a full change point analysis on the running statistics starting from locating the optimal change points given  $k$ , significance testing if  $k>0$ , and finally, determining the most optimal  $k$ . This function calls the function [kcpa](#) to find the most optimal change points given  $k$  and then the [permTest](#) function to carry out the permutation test. The model selection step is embedded in the `kcpRS` function.

This package also contains the function [kcpRS\\_workflow](#) which carries out a stepwise change point analysis to flag changes in 4 basic time series statistics: mean, variance, autocorrelation (lag 1) and correlations.

Two illustrative data sets are included: [MentalLoad](#) and [CO2Inhalation](#)

**Author(s)**

Jedelyn Cabrieto (<jed.cabrieto@kuleuven.be>) and Kristof Meers

For the core KCP analysis, the authors built upon the codes from the Supplementary Material available in doi:10.1080/01621459.2013.849605 by Matteson and James (2012).

**References**

Arlot, S., Celisse, A., & Harchaoui, Z. (2019). A kernel multiple change-point algorithm via model selection. *Journal of Machine Learning Research*, 20(162), 1-56.

Cabrieto, J., Tuerlinckx, F., Kuppens, P., Grassmann, M., & Ceulemans, E. (2017). Detecting correlation changes in multivariate time series: A comparison of four non-parametric change point detection methods. *Behavior Research Methods*, 49, 988-1005. doi:10.3758/s13428-016-0754-9

Cabrieto, J., Tuerlinckx, F., Kuppens, P., Hunyadi, B., & Ceulemans, E. (2018). Testing for the presence of correlation changes in a multivariate time series: A permutation based approach. *Scientific Reports*, 8, 769, 1-20. doi:10.1038/s41598-017-19067-2

Cabrieto, J., Tuerlinckx, F., Kuppens, P., Wilhelm, F., Liedlgruber, M., & Ceulemans, E. (2018). Capturing correlation changes by applying kernel change point detection on the running correlations. *Information Sciences*, 447, 117-139. doi:10.1016/j.ins.2018.03.010

Cabrieto, J., Adolf, J., Tuerlinckx, F., Kuppens, P., & Ceulemans, E. (2018). Detecting long-lived autodependency changes in a multivariate system via change point detection and regime switching models. *Scientific Reports*, 8, 15637, 1-15. doi:10.1038/s41598-018-33819-8

**See Also**

[kcpRS](#)

[kcpRS\\_workflow](#)

[MentalLoad](#)

[CO2Inhalation](#)

---

CO2Inhalation

*CO2 Inhalation Data*

---

**Description**

Nine physiological measures during a CO2-inhalation experiment.

**Usage**

```
data(CO2Inhalation)
```

**Format**

Dataframe with 239 rows and 10 columns. The first column indicates the experimental phase and the last nine columns correspond to the nine physiological measures tracked during the experiment: Breathing volume variables (ViVol, VeVol, Vent, PiaAB), breathing duration variables (Ti,Te,Tt), heart rate (HR) and RR interval (RR) or cardiac beat interval.

## References

De Roover, K., Timmerman, M. E., Van Diest, I., Onghena, P., & Ceulemans, E. (2014). Switching principal component analysis for modeling means and covariance changes over time. *Psychological Methods*, 19, 113-132. doi:10.1037/a0034525

## Examples

```
data(CO2Inhalation)
```

---

getScatterMatrix	<i>Get the matrix of optimized scatters used in locating the change points.</i>
------------------	---

---

## Description

Get the matrix of optimized scatters used in locating the change points.

## Usage

```
getScatterMatrix(II_, X_, H_)
```

## Arguments

II_	A $D \times N$ matrix where $D$ is the maximum no. of segments ( $K_{max}+1$ ) and $N$ is the no. of windows
X_	An $N \times r$ dataframe where $N$ is the no. of windows and $r$ the no. of running statistics monitored
H_	A $D \times N$ matrix where $D$ is the maximum no. of segments ( $K_{max}+1$ ) and $N$ is the no. of windows

## Value

II	A matrix of optimized scatters
H	A matrix of candidate changes point locations
medianK	Median of the pairwise Euclidean distances

---

kcpa *KCP (Kernel Change Point) Detection*

---

### Description

Finds the most optimal change point(s) in the running statistic time series `RunStat` by looking at their kernel-based pairwise similarities.

### Usage

```
kcpa(RunStat, Kmax = 10, wsize = 25)
```

### Arguments

<code>RunStat</code>	Dataframe of running statistics with rows corresponding to the windows and the columns corresponding to the variable(s) on which these running statistics were computed.
<code>Kmax</code>	Maximum number of change points
<code>wsize</code>	Window size

### Value

<code>kcpSoln</code>	A matrix comprised of the minimized variance criterion <i>Rmin</i> and the optimal change point location(s) for each <i>k</i> from 1 to <i>Kmax</i>
----------------------	---

### References

Arlot, S., Celisse, A., & Harchaoui, Z. (2019). A kernel multiple change-point algorithm via model selection. *Journal of Machine Learning Research*, 20(162), 1-56.

Cabrieto, J., Tuerlinckx, F., Kuppens, P., Grassmann, M., & Ceulemans, E. (2017). Detecting correlation changes in multivariate time series: A comparison of four non-parametric change point detection methods. *Behavior Research Methods*, 49, 988-1005. doi:10.3758/s13428-016-0754-9

---

kcpRS *KCP on the running statistics*

---

### Description

Given a user-specified function `RS_fun` to compute the running statistics (see [runMean](#), [runVar](#), [runAR](#) and [runCorr](#)), a KCP permutation test (see [permTest](#)) is first implemented to test whether there is at least one significant change point, then through model selection most optimal number of change points is chosen.

**Usage**

```

kcpRS(
  data,
  RS_fun,
  RS_name,
  wsize = 25,
  nperm = 1000,
  Kmax = 10,
  alpha = 0.05,
  varTest = FALSE,
  ncpu = 1
)

## S3 method for class 'kcpRS'
plot(x, ...)

## S3 method for class 'kcpRS'
print(x, kcp_details = TRUE, ...)

## S3 method for class 'kcpRS'
summary(object, ...)

```

**Arguments**

data	data $N \times v$ dataframe where $N$ is the number of time points and $v$ the number of variables
RS_fun	Running statistics function: Should require <code>wsize</code> and <code>wstep</code> as input and return a dataframe of running statistics as output. The rows of this dataframe should correspond to the windows and the columns should correspond to the variable(s) on which the running statistics were computed.
RS_name	Name of the monitored running statistic.
wsize	Window size
nperm	Number of permutations used in the permutation test
Kmax	Maximum number of change points desired
alpha	Significance level of the permutation test
varTest	If set to <code>FALSE</code> , only the variance DROP test is implemented, and if set to <code>TRUE</code> , both the variance test and the variance DROP tests are implemented.
ncpu	number of cpu cores to use
x	An object of the type produced by <code>kcpRS</code>
...	Further plotting arguments.
kcp_details	If <code>TRUE</code> , then the matrix of optimal change points solutions given $k$ is displayed. If <code>FALSE</code> , then this output is suppressed.
object	An object of the type produced by <code>kcpRS_workflow</code>

**Value**

RS_name	Name indicated for the monitored running statistic
RS	Dataframe of running statistics with rows corresponding to the time window and columns corresponding to the (combination of) variable(s) on which the running statistics were computed
wsiz	Selected window size
varTest	Selected choice of implementation for varTest
nperm	Selected number of permutations
alpha	Selected significance level of the permutation test
subTest_alpha	Significance level of each subtest. If varTest=0, subTest_alpha is equal to alpha since only the variance drop test is implemented. If varTest=1, subTest_alpha=alpha/2 since two subtests are carried out and Bonferonni correction is applied.
BestK	Optimal number of change points based on grid search
changePoints	Change point location(s)
p_var_test	P-value of the variance test
p_varDrop_test	P-value of the variance drop test
CPS_given_K	A matrix comprised of the minimized variance criterion $Rmin$ and the optimal change point location(s) for each $k$ from 1 to $Kmax$
changePoints_scee_test	Optimal number of change points based on scree test
scee_test	A matrix comprised of the scree values for each $k$ from 1 to $Kmax-1$
medianK	Median Euclidean distance between all pairs of running statistics

**References**

- Cabrieto, J., Tuerlinckx, F., Kuppens, P., Wilhelm, F., Liedlgruber, M., & Ceulemans, E. (2018). Capturing correlation changes by applying kernel change point detection on the running correlations. *Information Sciences*, 447, 117-139. doi:10.1016/j.ins.2018.03.010
- Cabrieto, J., Adolf, J., Tuerlinckx, F., Kuppens, P., & Ceulemans, E. (2018). Detecting long-lived autodependency changes in a multivariate system via change point detection and regime switching models. *Scientific Reports*, 8, 15637, 1-15. doi:10.1038/s41598-018-33819-8
- Cabrieto, J., Meers, K., Schat, E., Adolf, J. K., Kuppens, P., Tuerlinckx, F., & Ceulemans, E. (2022). kcpRS: An R package for performing kernel change point detection on the running statistics of multivariate time series. *Behavior Research Methods*, 54, 1092-1113. doi:10.3758/s13428-021-01603-8

**Examples**

```

phase1=cbind(rnorm(50,0,1),rnorm(50,0,1)) #phase1: Means=0
phase2=cbind(rnorm(50,1,1),rnorm(50,1,1)) #phase2: Means=1
X=rbind(phase1,phase2)
res=kcpRS(data=X,RS_fun=runMean,RS_name="Mean",wsiz=25,
nperm=1000,Kmax=10,alpha=.05,varTest=FALSE,ncpu=1)

```

```
summary(res)
plot(res)
```

---

kcpRS\_workflow

*KCP on the Running Statistics Workflow*


---

## Description

Any of the four basic running statistics (i.e., running means, running variances, running autocorrelations and running correlations) or a combination thereof can be scanned for change points.

## Usage

```
kcpRS_workflow(
  data,
  RS_funs = c("runMean", "runVar", "runAR", "runCorr"),
  wsize = 25,
  nperm = 1000,
  Kmax = 10,
  alpha = 0.05,
  varTest = FALSE,
  bcorr = TRUE,
  ncpu = 1
)

## S3 method for class 'kcpRS_workflow'
plot(x, ...)

## S3 method for class 'kcpRS_workflow'
print(x, ...)

## S3 method for class 'kcpRS_workflow'
summary(object, ...)
```

## Arguments

data	data $N \times v$ dataframe where $N$ is the number of time points and $v$ the number of variables
RS_funs	a vector of names of the functions that correspond to the running statistics to be monitored. Options available: "runMean"=running mean, "runVar"=running variance, "runAR"=running autocorrelation and "runCorr"=running correlation.
wsize	Window size
nperm	Number of permutations used in the permutation test
Kmax	Maximum number of change points desired



alpha	Significance level for the full KCP-RS workflow analysis if bcorr=1. Otherwise, this is the significance level for each running statistic.
varTest	If set to TRUE, only the variance DROP test is implemented, and if set to FALSE, both the variance test and the variance DROP tests are implemented.
bcorr	Set to TRUE if Bonferonni correction is desired for the workflow analysis and set to FALSE otherwise.
ncpu	number of cpu cores to use
x	An object of the type produced by kcpRS_workflow
...	Further plotting arguments
object	An object of the type produced by kcpRS_workflow

### Details

The workflow proceeds in two steps: First, the mean change points are flagged using KCP on the running means. If there are significant change points, the data is centered based on the yielded change points. Otherwise, the data remains untouched for the next analysis. Second, the remaining running statistics are computed using the centered data in the first step. The user can specify which running statistics to scan change points for (see `RS_funs` and examples). Bonferonni correction for tracking multiple running statistics can be implemented using the `bcorr` option.

### Value

kcpMean	kcpRS solution for the running means. See output of <a href="#">kcpRS</a> for further details.
kcpVar	kcpRS solution for the running variances. See output of <a href="#">kcpRS</a> for further details.
kcpAR	kcpRS solution for the running autocorrelations. See output of <a href="#">kcpRS</a> for further details.
kcpCorr	kcpRS solution for the running correlations. See output of <a href="#">kcpRS</a> for further details.

### References

Cabrieto, J., Adolf, J., Tuerlinckx, F., Kuppens, P., & Ceulemans, E. (2019). An objective, comprehensive and flexible statistical framework for detecting early warning signs of mental health problems. *Psychotherapy and Psychosomatics*, 88, 184-186. doi:10.1159/000494356

### Examples

```

phase1=cbind(rnorm(50,0,1),rnorm(50,0,1)) #phase1: Means=0
phase2=cbind(rnorm(50,1,1),rnorm(50,1,1)) #phase2: Means=1
X=rbind(phase1,phase2)

#scan all statistics

res=kcpRS_workflow(data=X,RS_funs=c("runMean","runVar","runAR","runCorr"),
wsize=25,nperm=1000,Kmax=10,alpha=.05, varTest=FALSE, bcorr=TRUE, ncpu=1)
summary(res)
plot(res)

```

```
#scan the mean and the correlation only
res=kcpRS_workflow(data=X,RS_funs=c("runMean","runCorr"),wsize=25,nperm=1000,Kmax=10,
  alpha=.05, varTest=FALSE, bcorr=TRUE, ncpu=1)
summary(res)
plot(res)
```

---

MentalLoad

*Mental Load Data*


---

### Description

Three physiological measures during a mental load assessment experiment on aviation pilots

### Usage

```
data(MentalLoad)
```

### Format

Dataframe with 1393 rows and 4 columns. The first column indicates the experimental period, while the last three columns correspond to the three physiological measures monitored during the experiment: Heart rate (HR), respiration rate (RR) and petCO2.

### References

Grassmann, M., Vlemincx, E., von Leupoldt, A., & Van den Bergh, O. (2016). The role of respiratory measures to assess mental load in pilot selection. *Ergonomics*, 59(6), 745-753. ([PubMed](#))

### Examples

```
data(MentalLoad)
```

---

permTest

*KCP Permutation Test*


---

### Description

The KCP permutation test implements the variance test and the variance drop test to determine if there is at least one change point in the running statistics

**Usage**

```
permTest(
  data,
  RS_fun,
  wsize = 25,
  nperm = 1000,
  Kmax = 10,
  alpha = 0.05,
  varTest = FALSE
)
```

**Arguments**

data	data $N \times v$ dataframe where $N$ is the number of time points and $v$ the number of variables
RS_fun	Running statistics function: Should require the time series and wsize as input and return a dataframe of running statistics as output. This output dataframe should have rows that correspond to the time windows and columns that correspond to the variable(s) on which the running statistics were computed.
wsize	Window size
nperm	Number of permutations to be used in the permutation test
Kmax	Maximum number of change points desired
alpha	Significance level of the permutation test
varTest	If FALSE, only the variance DROP test is implemented, and if TRUE, both the variance and the variance DROP tests are implemented.

**Value**

sig	Significance of having at least one change point. 0 - Not significant, 1- Significant
p_var_test	P-value of the variance test.
p_varDrop_test	P-value of the variance drop test.
perm_rmin	A matrix of minimized variance criterion for the permuted data.
perm_rmin_without_NA	A matrix of minimized variance criterion for the permuted data without NA values.

**References**

Cabrieto, J., Tuerlinckx, F., Kuppens, P., Hunyadi, B., & Ceulemans, E. (2018). Testing for the presence of correlation changes in a multivariate time series: A permutation based approach. *Scientific Reports*, 8, 769, 1-20. doi:10.1038/s41598-017-19067-2

---

runAR	<i>Running Autocorrelations</i>
-------	---------------------------------

---

**Description**

Extracts the running autocorrelations by sliding a window comprised of `wsiz` time points, and in each window, the autocorrelation for each variable is computed. Each time the window is slid, the oldest time point is discarded and the latest time point is added.

**Usage**

```
runAR(data, wsiz = 25)
```

**Arguments**

<code>data</code>	$N \times v$ dataframe where $N$ is the no. of time points and $v$ the no. of variables
<code>wsiz</code>	Window size

**Value**

Running autocorrelations time series

**Examples**

```
phase1=cbind(rnorm(50,0,1),rnorm(50,0,1)) #phase1: AutoCorr=0
phase2=cbind(rnorm(50,0,1),rnorm(50,0,1))
phase2=filter(phase2,.50, method="recursive") #phase2: AutoCorr=.5
X=rbind(phase1,phase2)
RS=runAR(data=X,wsiz=25)
ts.plot(RS, gpars=list(xlab="Window", ylab="Autocorrelation", col=1:2,lwd=2))
```

---

runCorr	<i>Running Correlations</i>
---------	-----------------------------

---

**Description**

Extracts the running correlations by sliding a window comprised of `wsiz` time points, and in each window, the correlation of each pair of variables is computed. Each time the window is slid, the oldest time point is discarded and the latest time point is added.

**Usage**

```
runCorr(data, wsiz = 25)
```

**Arguments**

data             $N \times v$  dataframe where  $N$  is the no. of time points and  $v$  the no. of variables  
 wsize           window size

**Value**

Running correlations time series

**Examples**

```
data(MentalLoad)
RS<-runCorr(data=MentalLoad,wsiz=25)
ts.plot(RS, gpars=list(xlab="Window", ylab="Correlations", col=1:3,lwd=2))
```

---

runMean	<i>Running Means</i>
---------	----------------------

---

**Description**

Extracts the running means by sliding a window comprised of `wsize` time points, and in each window, the mean for each variable is computed. Each time the window is slid, the oldest time point is discarded and the latest time point is added.

**Usage**

```
runMean(data, wsize = 25)
```

**Arguments**

data             $N \times v$  dataframe where  $N$  is the no. of time points and  $v$  the no. of variables  
 wsize           Window size

**Value**

Running means time series

**Examples**

```
phase1=cbind(rnorm(50,0,1),rnorm(50,0,1)) #phase1: Means=0
phase2=cbind(rnorm(50,1,1),rnorm(50,1,1)) #phase2: Means=1
X=rbind(phase1,phase2)
RS=runMean(data=X,wsiz=25)
ts.plot(RS, gpars=list(xlab="Window", ylab="Means", col=1:2,lwd=2))
```

---

runVar	<i>Running Variances</i>
--------	--------------------------

---

**Description**

Extracts the running variances by sliding a window comprised of `wsiz` time points, and in each window, the variance for each variable is computed. Each time the window is slid, the oldest time point is discarded and the latest time point is added.

**Usage**

```
runVar(data, wsiz = 25)
```

**Arguments**

<code>data</code>	$N \times v$ dataframe where $N$ is the no. of time points and $v$ the no. of variables
<code>wsiz</code>	Window size

**Value**

Running variances time series

**Examples**

```
phase1=cbind(rnorm(50,0,1),rnorm(50,0,1)) #phase1: SD=1
phase2=cbind(rnorm(50,0,2),rnorm(50,0,2)) #phase2: SD=2
X=rbind(phase1,phase2)
RS=runVar(data=X,wsiz=25)
ts.plot(RS, gpars=list(xlab="Window", ylab="Variances", col=1:2,lwd=2))
```

# Index

## \* datasets

CO2Inhalation, 3

MentalLoad, 10

CO2Inhalation, 2, 3, 3

getScatterMatrix, 4

kcpa, 2, 5

kcpRS, 2, 3, 5, 9

kcpRS-package, 2

kcpRS\_workflow, 2, 3, 8

MentalLoad, 2, 3, 10

permTest, 2, 5, 10

plot.kcpRS (kcpRS), 5

plot.kcpRS\_workflow (kcpRS\_workflow), 8

print.kcpRS (kcpRS), 5

print.kcpRS\_workflow (kcpRS\_workflow), 8

runAR, 2, 5, 12

runCorr, 2, 5, 12

runMean, 2, 5, 13

runVar, 2, 5, 14

summary.kcpRS (kcpRS), 5

summary.kcpRS\_workflow  
(kcpRS\_workflow), 8