

Normal Distribution

Density: $f(x) = \frac{1}{\sqrt{2\pi}\sigma} \exp\left[-\frac{1}{2}\left(\frac{x-\mu}{\sigma}\right)^2\right], \quad \int_{-\infty}^{\infty} f(x) dx = 1$

$$E[x] = \mu, \quad V[x] = \sigma^2, \quad CV[x] = \frac{\sigma}{\mu}$$

Lognormal Distribution

Density: $f(x) = \frac{1}{\sqrt{2\pi}\sigma x} \exp\left[-\frac{1}{2}\left(\frac{\log x - \mu}{\sigma}\right)^2\right], \quad \int_0^{\infty} f(x) dx = 1$

$$E[\log x] = \mu, \quad V[\log x] = \sigma^2, \quad CV[\log x] = \frac{\sigma}{\mu}$$

$$E[x] = \exp\left(\mu + \frac{\sigma^2}{2}\right), \quad V[x] = \exp(2\mu + \sigma^2) [\exp(\sigma^2) - 1],$$

$$CV[x] = \sqrt{\exp(\sigma^2) - 1}$$

Gamma Distribution

Density: $f(x) = \frac{x^{a-1}}{\Gamma(a)s^a} \exp\left(-\frac{x}{s}\right), \quad \int_0^{\infty} f(x) dx = 1$

Parameters: $a = \text{shape}, s = \text{scale}$

$$E[x] = as, \quad V[x] = as^2, \quad CV[x] = \sqrt{\frac{1}{a}}$$