

gMCP - an R package for a graphical approach to weighted multiple test procedures

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1 Introduction

This package provides functions and graphical user interfaces for graph based multiple test procedures. These graphs define a weighting strategy for all subsets of null hypotheses and following the closed test procedure weighted tests can be performed on these subsets leading to a multiple test

procedure controlling the family wise error rate in the strong sense. In some cases shortcuts are available, for example the weighted Bonferroni procedure leads to a sequentially rejective multiple test procedure.

At all steps either graphical user interfaces or the R Console with S4 objects and methods can be used.

Please note that this is still a beta release and the API will most likely still change in future versions.

1.1 Example and diving in

Let's start with a well-known procedure and see how it fits into this graphical approach to weighted multiple test procedures: The Bonferroni-Holm-Procedure [6].

Theorem 1.1 (Bonferroni-Holm-Procedure). *Let T_1, \dots, T_m be test statistics for $m \in \mathbb{N}$ null hypotheses H_1, \dots, H_m and p_1, \dots, p_m the associated p -values. Then the following test will control the familywise error rate at level $\alpha \in]0, 1[$ in the strong sense:*

Denote the ordered p -values by $p^{(1)} < p^{(2)} < \dots < p^{(m)}$ and the corresponding hypotheses by $H^{(1)}, H^{(2)}, \dots, H^{(m)}$.

Reject $H^{(1)}, H^{(2)}, \dots, H^{(j)}$ such that

$$p^{(i)} \leq \frac{\alpha}{n - i + 1} \quad \text{for all } 1 \leq i \leq j.$$

The corresponding graph for the Bonferroni-Holm-Procedure for three hypotheses is given in Figure 1. We see a fully connected graph, where each node represents a hypothesis and the nodes and edges have weights.

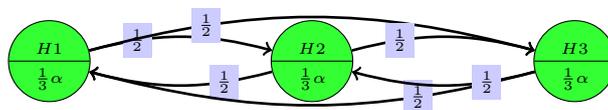


Figure 1: Graph representing the Bonferroni-Holm-Procedure for three hypotheses.

A null hypothesis can be rejected, when the p -value is less than the alpha level of the corresponding node. In this case the graph will be updated and the alpha level of this node is passed according to the edge weights.

Example 1.2. We give an example for the Bonferroni-Holm-Procedure that will be used repeatedly throughout this manual. Of course this package is made for more advanced tests (you find a selection in section 7), but since most readers are already familiar with this procedure, for a first introduction of `gMCP`, we stick to this simple example.

Let $p_1 = 0.01$, $p_2 = 0.07$ and $p_3 = 0.02$ be three p -values and $\alpha = 0.05$. In the first step H_1 can be rejected since $p_1 < \alpha/3$. The updated graph can be seen in figure 2 and now also H_3 can be rejected since $p_1 < \alpha/2$. Again the graph is updated, but H_2 can not be rejected.

Let's reproduce this with the `gMCP` package. We start R and enter:

```
> library(gMCP)
> graphGUI()
```

The GUI seen in Figure 4 is shown and we select from the menu "Example graphs" the entry "Bonferroni-Holm Test". We enter the three p -values in the respective fields on the right side. By clicking on the button with the green arrow we start the test procedure and can sequentially reject all three hypotheses.

If we don't want to use the GUI we can also use R:

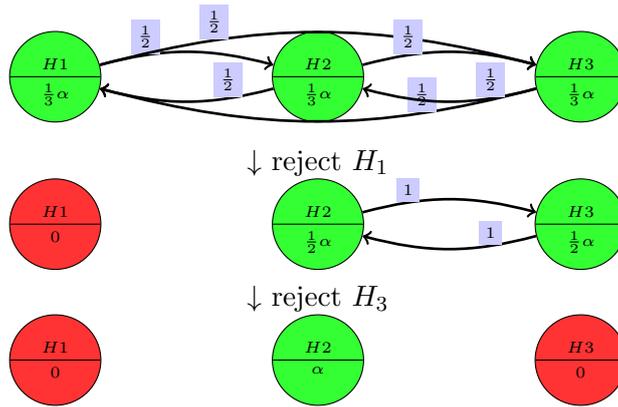


Figure 2: Example showing how two null hypotheses can be rejected with p-values $p_1 = 0.01$, $p_2 = 0.07$ and $p_3 = 0.02$.

```
> library(gMCP)
> graph <- createBonferroniHolmGraph(3)
> gMCP(graph, pvalues = c(0.01, 0.07, 0.02), alpha = 0.05)
```

gMCP-Result

Initial graph:

A graphMCP graph

H1 (not rejected, weight=0.3333)

H2 (not rejected, weight=0.3333)

H3 (not rejected, weight=0.3333)

Edges:

H1 -(1/2)-> H2

H1 -(1/2)-> H3

H2 -(1/2)-> H1

H2 -(1/2)-> H3

H3 -(1/2)-> H1

H3 -(1/2)-> H2

P-values:

H1 H2 H3

0.01 0.07 0.02

Adjusted p-values:

H1 H2 H3

0.03 0.07 0.04

Alpha: 0.05

Hypothesis rejected:

H1 H2 H3

TRUE FALSE TRUE

Final graph after 2 steps:

A graphMCP graph

H1 (rejected, weight=0)

H2 (not rejected, weight=1)

H3 (rejected, weight=0)

No edges.

2 Creating the graph

In the first step a graph that describes the multiple test procedures must be created.

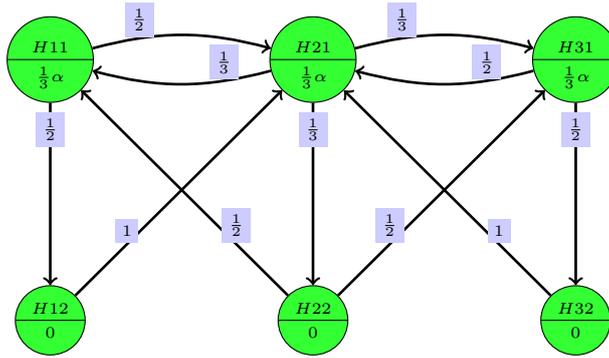


Figure 3: Example graph from [2] that we will create in this vignette.

2.1 Using R

We build upon the package `graph` [4], more precisely we declare a new class `graphMCP` that is a subclass of `graphNEL`. The `initialize` method of this subclass differs only in an extra argument `alpha`, the initial allocation of the significance level `alpha` to the individual hypotheses. Declaration of the nodes and edges is inherited from class `graphNEL`.

As an example we now create the graph from Bretz et al. [2] that you can see in figure 3.

```
> hnodes <- c("H11", "H21", "H31", "H12", "H22", "H32")
> weights <- c(1/3, 1/3, 1/3, 0, 0, 0)
> edges <- list()
> edges[["H11"]] <- list(edges = c("H21", "H12"), weights = c(1/2, 1/2))
> edges[["H21"]] <- list(edges = c("H11", "H31", "H22"), weights = c(1/3, 1/3, 1/3))
> edges[["H31"]] <- list(edges = c("H21", "H32"), weights = c(1/2, 1/2))
> edges[["H12"]] <- list(edges = "H21", weights = 1)
> edges[["H22"]] <- list(edges = c("H11", "H31"), weights = c(1/2, 1/2))
> edges[["H32"]] <- list(edges = "H21", weights = 1)
> graph <- new("graphMCP", nodes = hnodes, edgeL = edges, weights = weights)
```

Let's print the newly created graph:

```
> print(graph)

A graphMCP graph
H11 (not rejected, weight=0.3333)
H21 (not rejected, weight=0.3333)
H31 (not rejected, weight=0.3333)
H12 (not rejected, weight=0)
H22 (not rejected, weight=0)
H32 (not rejected, weight=0)
Edges:
H11 -( 1/2 )-> H21
H11 -( 1/2 )-> H12
H21 -( 1/3 )-> H11
H21 -( 1/3 )-> H31
H21 -( 1/3 )-> H22
H31 -( 1/2 )-> H21
H31 -( 1/2 )-> H32
H12 -( 1 )-> H21
H22 -( 1/2 )-> H11
H22 -( 1/2 )-> H31
H32 -( 1 )-> H21
```

Since we also want to visualize the graph, we use the method `nodeRenderInfo` from package `graph` to set appropriate x- and y-coordinates in the `renderInfo`. (We are compatible to the `renderInfo` usage from package `Rgraphviz` [5].)

```
> nodeX <- c(H11 = 100, H21 = 300, H31 = 500, H12 = 100, H22 = 300, H32 = 500)
> nodeY <- c(H11 = 100, H21 = 100, H31 = 100, H12 = 300, H22 = 300, H32 = 300)
> nodeRenderInfo(graph) <- list(nodeX = nodeX, nodeY = nodeY)
```

Coordinates are interpreted as pixels in the GUI and big points in L^AT_EX (72 bp = 1 inch).

Let's take a look at the graph in L^AT_EX rendered with TikZ [8] (you can see the compiled result in figure 3):

```
> cat(graph2latex(graph))

\begin{tikzpicture}[scale=1]
\node (H11) at (100bp,-100bp)[draw,circle split,fill=green!80] {$H11$ \nodepart{lower} $\frac{1}{3}\alpha$};
\node (H21) at (300bp,-100bp)[draw,circle split,fill=green!80] {$H21$ \nodepart{lower} $\frac{1}{3}\alpha$};
\node (H31) at (500bp,-100bp)[draw,circle split,fill=green!80] {$H31$ \nodepart{lower} $\frac{1}{3}\alpha$};
\node (H12) at (100bp,-300bp)[draw,circle split,fill=green!80] {$H12$ \nodepart{lower} $0$};
\node (H22) at (300bp,-300bp)[draw,circle split,fill=green!80] {$H22$ \nodepart{lower} $0$};
\node (H32) at (500bp,-300bp)[draw,circle split,fill=green!80] {$H32$ \nodepart{lower} $0$};
\draw [->,line width=1pt] (H11) to[bend left=15] node[near start,above,fill=blue!20] {$\frac{1}{2}$} (H21);
\draw [->,line width=1pt] (H11) to[auto] node[near start,above,fill=blue!20] {$\frac{1}{2}$} (H12);
\draw [->,line width=1pt] (H21) to[bend left=15] node[near start,above,fill=blue!20] {$\frac{1}{3}$} (H11);
\draw [->,line width=1pt] (H21) to[bend left=15] node[near start,above,fill=blue!20] {$\frac{1}{3}$} (H31);
\draw [->,line width=1pt] (H21) to[auto] node[near start,above,fill=blue!20] {$\frac{1}{3}$} (H22);
\draw [->,line width=1pt] (H31) to[bend left=15] node[near start,above,fill=blue!20] {$\frac{1}{2}$} (H21);
\draw [->,line width=1pt] (H31) to[auto] node[near start,above,fill=blue!20] {$\frac{1}{2}$} (H32);
\draw [->,line width=1pt] (H12) to[auto] node[near start,above,fill=blue!20] {$1$} (H21);
\draw [->,line width=1pt] (H22) to[auto] node[near start,above,fill=blue!20] {$\frac{1}{2}$} (H11);
\draw [->,line width=1pt] (H22) to[auto] node[near start,above,fill=blue!20] {$\frac{1}{2}$} (H31);
\draw [->,line width=1pt] (H32) to[auto] node[near start,above,fill=blue!20] {$1$} (H21);
\end{tikzpicture}
```

We can even change the position of the edge labels for further fine tuning of the graphical representation. With the following command we place the label for the edge from H1 to H2 at position (200, 80):

```
> edgeData(graph, "H11", "H21", "labelX") <- 200
> edgeData(graph, "H11", "H21", "labelY") <- 80
```

2.1.1 graph2matrix and matrix2graph

We can also construct a graph from a given adjacency matrix via the command `matrix2graph`:

```
> m <- matrix(rep(1/3, 16), nrow = 4)
> diag(m) <- c(0, 0, 0, 0)
> graph <- matrix2graph(m)
> print(graph)
```

```
A graphMCP graph
H1 (not rejected, weight=0.25)
H2 (not rejected, weight=0.25)
H3 (not rejected, weight=0.25)
H4 (not rejected, weight=0.25)
Edges:
H1 -( 1/3 )-> H2
H1 -( 1/3 )-> H3
H1 -( 1/3 )-> H4
H2 -( 1/3 )-> H1
H2 -( 1/3 )-> H3
H2 -( 1/3 )-> H4
H3 -( 1/3 )-> H1
H3 -( 1/3 )-> H2
H3 -( 1/3 )-> H4
H4 -( 1/3 )-> H1
H4 -( 1/3 )-> H2
H4 -( 1/3 )-> H3
```

```
> graph2matrix(graph)
```

```
      H1      H2      H3      H4
H1 0.0000 0.3333 0.3333 0.3333
H2 0.3333 0.0000 0.3333 0.3333
H3 0.3333 0.3333 0.0000 0.3333
H4 0.3333 0.3333 0.3333 0.0000
```

2.2 Using the GUI

The creation of `graphMCP` objects as seen in the last section with basic R commands is very straight forward, but still takes some time and typos may occur. More convenient for the average user is the use of the graphical user interface for creating and editing MCP graphs that the `gMCP` package includes.

It is called by the command `graphGUI()` and takes as optional argument a variable name, given as a character string, of the graph to edit or under which a newly created `graphMCP` object will be available from the R command line.

```
> graphGUI("graph")
```

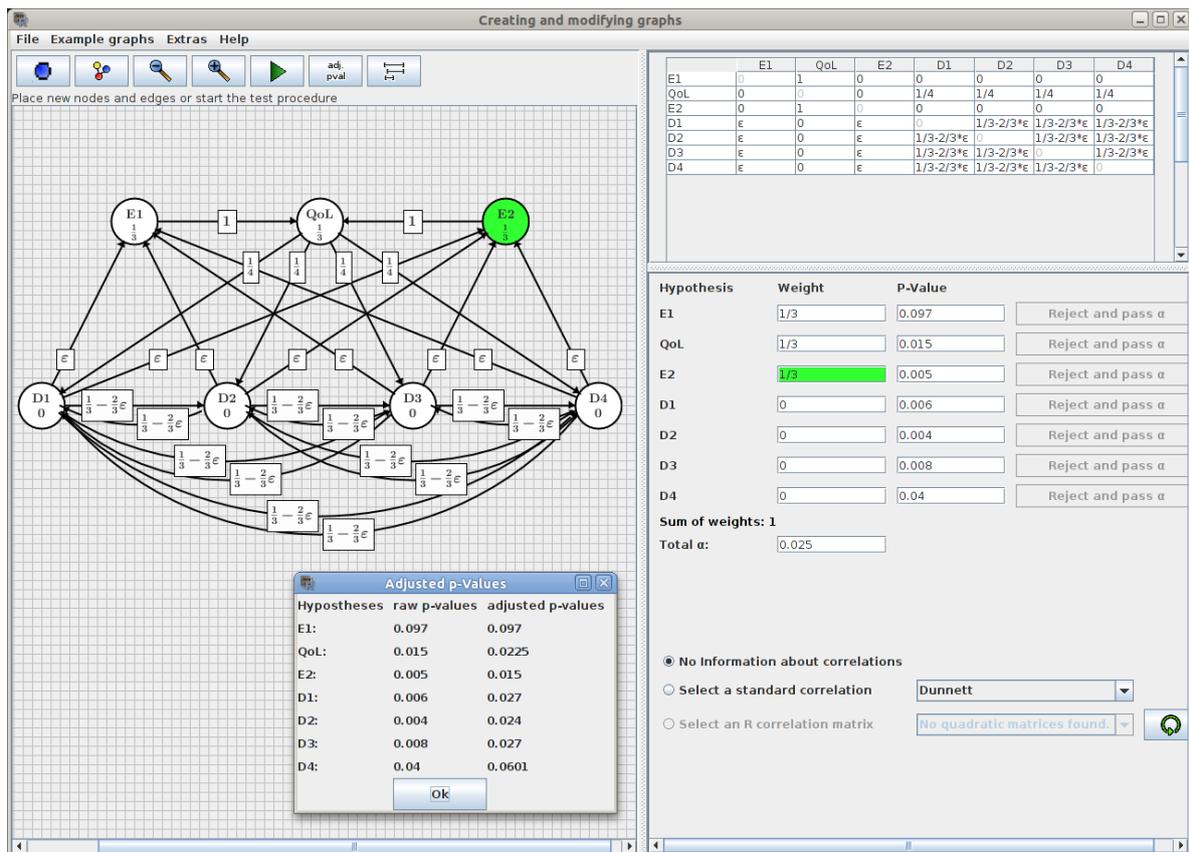


Figure 4: The graphical user interface allows testing, calculation of confidence intervals and adjusted p-values.

Let's take a look at the icon panel:



This button lets you add a new node to the graph. After pressing the button click somewhere on the graph panel and a new node will appear at this place.



This button lets you add a new edge between two nodes. After pressing the button click on the node the edge should start and after that on the node the edge should end.



For really big graphs the ability to zoom in and out is useful.



Starts the testing procedure / goes back to the graph modification.



Calculates the adjusted p-values.



Calculates simultaneous confidence intervals.

With drag and drop you can move nodes and also adjust edges.

3 The sequentially rejective MTP

For a full description of the sequentially rejective multiple testing procedure take a look at Bretz et al. [1].

3.1 Using R

You can either specify each rejection step yourself or simply use the method `gMCP`:

```
> graph <- createGraphFromBretzEtAl()
> # We can reject a single node:
> print(rejectNode(graph, "H11"))

A graphMCP graph
H11 (rejected, weight=0)
H21 (not rejected, weight=0.5)
H31 (not rejected, weight=0.3333)
H12 (not rejected, weight=0.1667)
H22 (not rejected, weight=0)
H32 (not rejected, weight=0)
Edges:
H21 -( 2/5 )-> H31
H21 -( 2/5 )-> H22
H21 -( 1/5 )-> H12
H31 -( 1/2 )-> H21
H31 -( 1/2 )-> H32
H12 -( 1 )-> H21
H22 -( 1/2 )-> H31
H22 -( 1/4 )-> H21
H22 -( 1/4 )-> H12
H32 -( 1 )-> H21

> # Or given a vector of pvalues let the function gMCP do all the work:
> pvalues <- c(0.1, 0.008, 0.005, 0.15, 0.04, 0.006)
> result <- gMCP(graph, pvalues)
> print(result)
```

`gMCP-Result`

```
Initial graph:
A graphMCP graph
H11 (not rejected, weight=0.3333)
H21 (not rejected, weight=0.3333)
H31 (not rejected, weight=0.3333)
H12 (not rejected, weight=0)
H22 (not rejected, weight=0)
H32 (not rejected, weight=0)
Edges:
H11 -( 1/2 )-> H21
H11 -( 1/2 )-> H12
H21 -( 1/3 )-> H11
H21 -( 1/3 )-> H31
H21 -( 1/3 )-> H22
H31 -( 1/2 )-> H21
H31 -( 1/2 )-> H32
H12 -( 1 )-> H21
H22 -( 1/2 )-> H11
H22 -( 1/2 )-> H31
H32 -( 1 )-> H21

P-values:
  H11  H21  H31  H12  H22  H32
0.100 0.008 0.005 0.150 0.040 0.006

Adjusted p-values:
  H11  H21  H31  H12  H22  H32
0.1200 0.0160 0.0150 0.1500 0.1200 0.0225

Alpha: 0.05
```

```
Hypothesis rejected:
  H11  H21  H31  H12  H22  H32
FALSE TRUE TRUE FALSE FALSE TRUE
```

```
Final graph after 3 steps:
A graphMCP graph
H11 (not rejected, weight=0.6667)
H21 (rejected, weight=0)
H31 (rejected, weight=0)
H12 (not rejected, weight=0)
H22 (not rejected, weight=0.3333)
H32 (rejected, weight=0)
Edges:
H11 -( 2/3 )-> H12
H11 -( 1/3 )-> H22
H12 -( 1/2 )-> H11
H12 -( 1/2 )-> H22
H22 -( 1 )-> H11
```

>

We can create a TikZ graphic from the last graph with `graph2latex(result@graphs[[4]])` that is shown in figure 5.

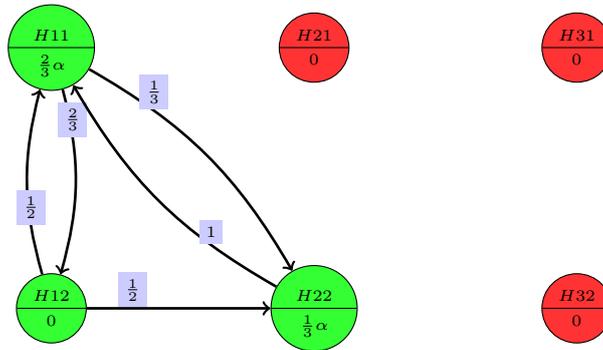


Figure 5: Final graph from the test procedure after rejection of H_{21} , H_{31} and H_{32} .

The command `gMCPReport` generates a full report of the testing procedure:

```
> gMCPReport(result, "Report.tex")
```

3.1.1 Adjusted p-values and simultaneous confidence intervals

Also adjusted p-values and simultaneous confidence intervals can be computed.

Let's assume the tests for hypotheses $H1 : \theta_1 \leq 0$, $H2 : \theta_2 \leq 0$ and $H3 : \theta_3 \leq 0$ are three t-tests with degree of freedom 9. The estimates are $\hat{\theta}_1 = 0.981$, $\hat{\theta}_2 = 1.089$ and $\hat{\theta}_3 = 0.8706$, the sample standard deviations $s_1 = 0.876$, $s_2 = 1.291$ and $s_3 = 0.8571$ the t-statistics 3.541, 2.666 and 3.212 and the corresponding p-values 0.0063, 0.02577 and 0.01062. We want to adjust for multiple testing by using the Bonferroni-Holm-Procedure with $\alpha = 0.025$.

```
> # Estimates:
> est <- c("H1"=0.860382, "H2"=0.9161474, "H3"=0.9732953)
> # Sample standard deviations:
> ssd <- c("H1"=0.8759528, "H2"=1.291310, "H3"=0.8570892)
> pval <- c(0.01260, 0.05154, 0.02124)/2
> simConfint(createBonferroniHolmGraph(3), pvalues=pval,
+             confint=function(node, alpha) {
+               c(est[node]-qt(1-alpha,df=9)*ssd[node]/sqrt(10), Inf)
+             }, alpha=0.025, mu=0, alternative="greater")
```

```

lower bound upper bound
H1      0.0000      Inf
H2     -0.0076      Inf
H3      0.0000      Inf

> # Note that the sample standard deviations will be calculated from the pvalues and estimates.
> # For example by estimates/dist(pvalues) for alternative="less".
> simConfint(createBonferroniHolmGraph(3), pvalues=pval,
+           confint="t", df=9, estimates=est, alpha=0.025, alternative="greater")

lower bound upper bound
[1,]    0.000000      Inf
[2,]   -0.007581      Inf
[3,]    0.000000      Inf

>

```

3.2 Using the GUI

Hypotheses	Initial alpha	Estimate	Standard error/deviation	Distribution	df	Alternative
H1:	α=0.3333	0.860382	0.27700059708019403	t-distributed	9	greater
H2:	α=0.3333	0.9161474	0.40834807653520294	t-distributed	9	greater
H3:	α=0.3333	0.9732953	0.2710354029931588	t-distributed	9	greater

Confidence Intervals:

H1:]0, ∞[
H2:] -0.0076, ∞[
H3:]0, ∞[

Figure 6: For normal and t-distributions simultaneous CI can be calculated by the GUI.

Use the following two buttons:  

See [3].

4 Weighted parametric tests

Figure 7: You can also specify a correlation between the tests.

In the lower right panel with p-values, it is also possible to specify a known correlation between these values (see figure 7).

For further information please take a look at the vignette "Weighted parametric tests defined by graphs".

5 Epsilon edges

The GUI supports epsilon edges. You can enter the weights in R syntax, e.g. $1 - 2e + \frac{1}{3}e^2$

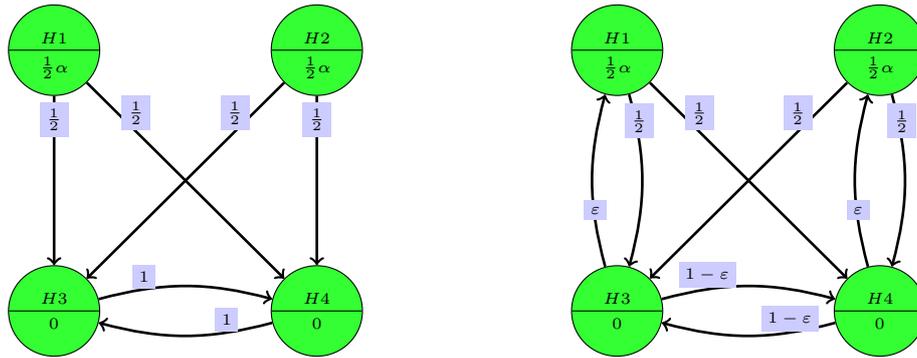


Figure 8: The Parallel Gatekeeping and the Improved Parallel Gatekeeping Procedure.

```

> graph <- createGraphForImprovedParallelGatekeeping()
> graph

A graphMCP graph
H1 (not rejected, weight=0.5)
H2 (not rejected, weight=0.5)
H3 (not rejected, weight=0)
H4 (not rejected, weight=0)
Edges:
H1 -( 1/2 )-> H3
H1 -( 1/2 )-> H4
H2 -( 1/2 )-> H3
H2 -( 1/2 )-> H4
H3 -( 1-e )-> H4
H3 -( e )-> H1
H4 -( 1-e )-> H3
H4 -( e )-> H2

> substituteEps(graph, eps=0.001)

A graphMCP graph
H1 (not rejected, weight=0.5)
H2 (not rejected, weight=0.5)
H3 (not rejected, weight=0)
H4 (not rejected, weight=0)
Edges:
H1 -( 1/2 )-> H3
H1 -( 1/2 )-> H4
H2 -( 1/2 )-> H3
H2 -( 1/2 )-> H4
H3 -( 999/1000 )-> H4
H3 -( 1/1000 )-> H1
H4 -( 999/1000 )-> H3
H4 -( 1/1000 )-> H2

> gMCP(graph, pvalues=c(0.02, 0.04, 0.01, 0.02), eps=0.001)

gMCP-Result

Initial graph:
A graphMCP graph
H1 (not rejected, weight=0.5)
H2 (not rejected, weight=0.5)
H3 (not rejected, weight=0)
H4 (not rejected, weight=0)
Edges:
H1 -( 1/2 )-> H3
H1 -( 1/2 )-> H4
H2 -( 1/2 )-> H3
H2 -( 1/2 )-> H4
H3 -( 1-e )-> H4
H3 -( e )-> H1
H4 -( 1-e )-> H3
H4 -( e )-> H2

```

```
P-values:  
  H1  H2  H3  H4  
0.02 0.04 0.01 0.02
```

```
Adjusted p-values:  
  H1  H2  H3  H4  
0.04 0.04 0.04 0.04
```

Alpha: 0.05

```
Hypothesis rejected:  
  H1  H2  H3  H4  
TRUE TRUE TRUE TRUE
```

```
Final graph after 4 steps:  
A graphMCP graph  
H1 (rejected, weight=0)  
H2 (rejected, weight=1)  
H3 (rejected, weight=0)  
H4 (rejected, weight=0)  
No edges.
```

>

6 Options and Import/Export

6.1 Options

This subsection is work in progress, but fortunately the options in figure 9 should be fairly self-explanatory.

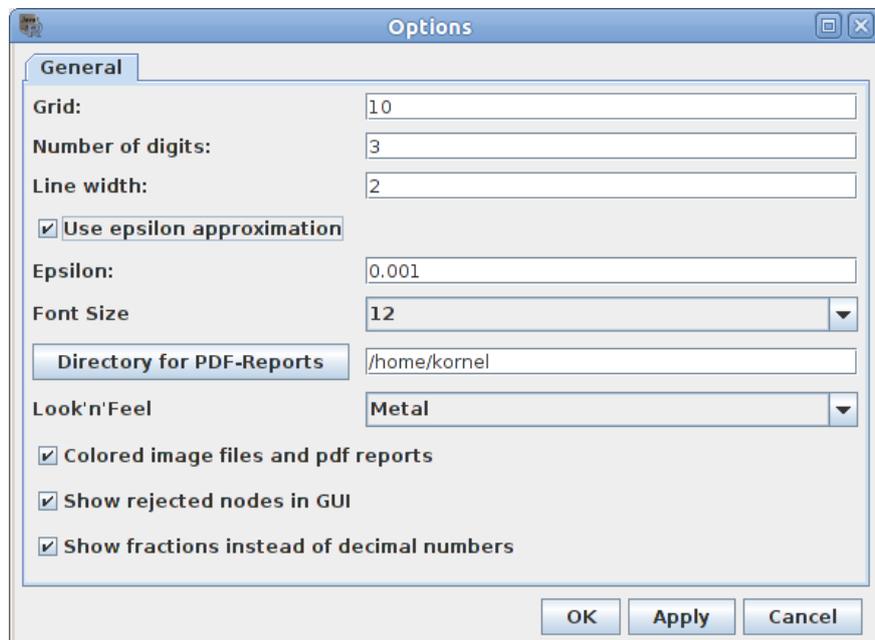


Figure 9: You can configure many things in the option dialog.

6.2 Import/Exports

This subsection is work in progress, but fortunately the menu entries in figure 10 should be fairly self-explanatory.

You can export graphs to png files. The background of these png files will be made transparent, so that they will fit into whichever document you insert them. Note that some image viewers visualize transparency with a checkerboard pattern.

File	Example graphs	Extras	Help
New Graph			
Load Graph from R			
Load Graph from RData file			
Save Graph to R			
Save Graph to RData file			
Export Graph to PNG Image			
Export Graph to LaTeX File			
Save LaTeX Report			
Save PDF Report			
Quit			

Figure 10: Import and export of graphs.

6.3 Important TikZ commands for optimizing the reports

A clear automatic placement of edges and weight labels without overlapping is a very difficult task and for complicated graphs the `gMCP` package will often fail to accomplish this. There is the possibility to adjust the edges and labels in the GUI, but since the \LaTeX graph layout is not (yet) exactly the same, there is perhaps the need for adjusting the graphs in the TikZ code. The TikZ program is very useful and we recommend it for many purposes, but perhaps you don't have the time to read the 560 pages manual [8], so here is a short overview of the most important commands for this kind of graphs.

Let's start with this graph in figure 11:

```
\begin{tikzpicture}[scale=1]
\node (H11) at (200bp,200bp) [draw,circle split,fill=green!80] {$H_{11}$ \nodepart{lower} $0.0333$};
...
\draw [->,line width=1pt] (H11) to[bend left=15] node[near start,above,fill=blue!20] {0.667} (H12);
...
\end{tikzpicture}
```

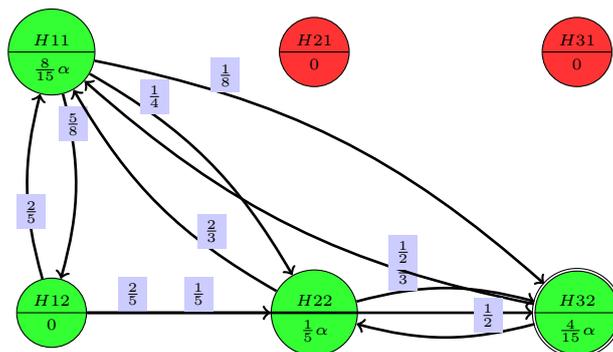


Figure 11: Graph from `graph2latex` that does not look optimal.

You can scale the TikZ graphic by changing the `[scale=1]` option. By default `graph2latex` doesn't scale TikZ graphics, but has an optional parameter `scale`.

For an explanation what `green!80` means and how you can specify other colors, please take a look at the `xcolor` manual [7].

You can choose between the following label positions `above`, `below`, `right`, `left`, `above right`, `above left`, `below right`, and `below left`. In addition these positions can take an optional dimension argument, so that for example `below=1pt` can be used to place a label below and additionally shift it 1pt downwards.

You can change the position where the edge weight label is placed to `at start`, `very near start`, `near start`, `midway`, `near end`, `very near end` and `at end` or simply use something like `pos=0.5`. If you add an argument `sloped`, the text label will be rotated so that a parallel line to the base line becomes a tangent to the edge.

Often it is useful to reduce the bending angle in `[bend left=15]` below 15. You could also specify and change `out=15` and `in=165` separately.

A powerful feature is the use of styles, since this will effect all objects of a given class. But for this please take a look directly at the TikZ manual [8].

7 Case Studies

This section is work in progress.

8 Appendix - Multiple Testing Basics

This section is work in progress.

Definition 8.1.

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